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Total Number of Pages: 02

Course: B.Tech
Sub_Code: RCS5C001/RCS5D007

5th Semester Back Examination: 2025-26

SUBJECT: Formal Languages and Automata Theory

BRANCH(S): CSE, CSEAIML, CSEDS, CSIT, CST, ELECTRICAL & C.E, IT, CSEAI

Time: 3 Hours

Max Marks: 100

Q.Code: U020

Answer Question No.1 (Part-I) which is compulsory, any eight from Part-II and any two from Part-III.

The figures in the right-hand margin indicate marks.

Part-I

Q1 Answer the following questions: (2 x 10)

- Differentiate between NFA and DFA.
- Explain the purpose of the Myhill–Nerode equivalence relation.
- List any two algebraic identities of regular expressions.
- What is an inherently ambiguous grammar? Give an example.
- What is a Universal Turing Machine?
- Describe closure under union for regular languages.
- Distinguish between deterministic and non-deterministic PDAs with examples.
- What is the Halting Problem? Why is it important?
- Define leftmost and rightmost derivation in a CFG.
- Explain Instantaneous Description (ID) for PDA.

Part-II

Q2 Only Focused-Short Answer Type Questions- (Answer Any Eight out of Twelve) (6 x 8)

- Construct a DFA for all binary strings containing an odd number of occurrences of substring "101"
- Convert the following NFA to an equivalent DFA:
States: $\{q_0, q_1\}$, Alphabet: $\{a, b\}$
Transition: $\delta(q_0, a) = \{q_0, q_1\}$, $\delta(q_0, b) = \{q_0\}$, $\delta(q_1, a) = \{q_1\}$, $\delta(q_1, b) = \emptyset$
- Convert the regular expression $(0+1)^*011$ into a minimal state automaton.
- Using the Pumping Lemma, show that $L = \{0^n 1^m 0^n \mid n, m \geq 1\}$ is not regular.
- Simplify the grammar and convert it into CNF: $S \rightarrow AS \mid aB$; $A \rightarrow aA \mid a$; $B \rightarrow bB \mid b$.
- Analyze why deterministic PDAs cannot recognize all CFLs with examples.
- Construct a PDA for $L = \{a^n b^n c^m \mid m, n \geq 1\}$ and explain acceptance by empty stack.
- Explain variants of Turing Machines.
- State and prove Kleene's Theorem.

- j) Derive a regular expression for the FA of a binary counter modulo 3.
- k) Prove every deterministic CFL is unambiguous; converse false.
- l) Construct a TM to compute $f(n) = 2n$ on unary input.

Part-III

Only Long Answer Type Questions (Answer Any Two out of Four)

- Q3** a) Create the minimal DFA for $L = \{w \in \{0,1\}^* \mid w \text{ interpreted as binary} \equiv 3 \pmod{7}\}$. (8)
- b) Prove the Myhill–Nerode condition and evaluate minimal DFA generation. (8)

- Q4** a) What is a Mealy Machine? Convert following Mealy Machine to Moore Machine. (8)

Present State	Next State			
	Input a = 0		Input a = 1	
	State	Output	State	Output
q ₁	q ₃	0	q ₂	0
q ₂	q ₁	1	q ₄	0
q ₃	q ₂	1	q ₁	1
q ₄	q ₄	1	q ₃	0

- b) Design a regular expression for binary strings divisible by 6 and justify correctness. (8)

- Q5** a) Convert $S \rightarrow aSbS \mid bSaS \mid \epsilon$ into CNF and evaluate blow-up. (8)
- b) Create an unambiguous grammar for $L = \{a^n b^n c^m \mid n, m \geq 1\}$ and justify correctness. (8)

- Q6** a) Explain how a TM computes integer functions. (8)
- b) Evaluate and prove that MPCP reduces to PCP. (8)