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Total Number of Pages : 02

B. Tech/ IDD (B.Tech and M.Tech)
RCS4C002 / RIT4C002

4th Semester Reg/Back Examination: 2023-24

Design and Analysis of Algorithm

CSE, IT, CSEAI, CSEAIME, CSEDS, CST, ELECTRICAL & C.E, ELECTRONICS & C.E

Time : 3 Hour

Max Marks : 100

Q. Code : P587

Answer Question No.1 (Part-1) which is compulsory, any eight from Part-II and any two from Part-III.

The figures in the right hand margin indicate marks.

Part-I

Q1 Answer the following questions:

(2 x 10)

- What is the running time of Quick sort when all elements of array **A** have the same value?
- The elements 61, 18, 25, 30, 90, 20 are inserted one by one in the given order into a Max Heap. The resultant Max Heap is
- Arrange the following functions in the increasing order of their growth.
 $\ln 2^n$, $n^{1.001}$, $n \log n$, e^n , n^{10}
- Give an asymptotic upper bound for the recurrence $T(n) = T(n-1) + n$.
- Why greedy algorithm cannot be applied to solve 0-1 knapsack problem?
- Formulate Longest Common Subsequence (LCS) as a dynamic programming.
- Write the recurrence equation to represent the time complexity of merge sort and solve it using Master method.
- What do you mean by heuristic approach?
- Define Max Clique problem.
- What is the difference between decision problem and optimization problem? Give an example of optimization problem and write its equivalent decision problem.

Part-II

Q2 Only Focused-Short Answer Type Questions- (Answer Any Eight out of Twelve)

(6 x 8)

- Solve the following recurrence equation: $T(n) = 5T(n/5) + \sqrt{n}$, $T(1) = 1$, $T(0) = 0$.
- Consider two strings $A = "qpqr"$ and $B = "pqprqp"$. Let x be the length of the longest common subsequence (not necessarily contiguous) between A and B and let y be the number of such longest common subsequences between A and B . Then compute the value of $x + 10y$. Adopt dynamic programming to find the longest common subsequence.
- Let A_1 , A_2 , A_3 , and A_4 be four matrices of dimensions 10×5 , 5×20 , 20×10 , and 10×5 , respectively. Calculate the minimum number of scalar multiplications required to find the product $A_1A_2A_3A_4$ using the basic matrix multiplication method. **Note** : Use dynamic programming for optimal parenthesization.

- d) A networking company uses a compression technique to encode the message before transmitting over the network. Suppose the message contains the following characters with their frequency:

character	a	b	c	d	e	f
Frequency	5	9	12	13	16	45

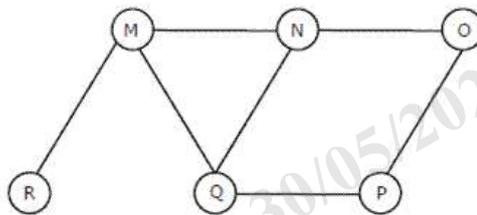
Note : Each character in input message takes 1 byte.

If the compression technique used is Huffman Coding, how many bits will be saved in the message?

- e) Give asymptotic upper bounds for $T(n)$ in each of the following recurrences. Assume that $T(n)$ is constant for sufficiently small n .

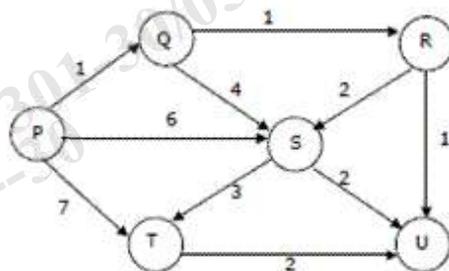
(i) $T(n) = T(n/2) + T(n/4) + T(n/8) + n$ (ii) $T(n) = 3T(n/4) + n^2$

- f) Apply Breadth First Search and Depth First Search algorithm to find all possible order of visiting the nodes of the following graph by taking M as the source vertex.



Let G be a graph with n vertices and m edges. What is the tightest upper bound on the running time on Breadth First Search and Depth First Search of G ? Assume that the graph is represented using adjacency matrix.

- g) Suppose we run Dijkstra's single source shortest-path algorithm on the following edge weighted directed graph with vertex P as the source. In what order do the nodes get included into the set of vertices for which the shortest path distances are finalized? Show all steps.



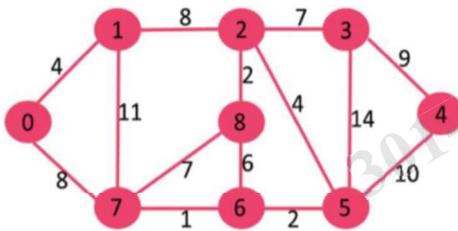
- h) Write the steps of solving a recurrence equation using the master method. Can the master method be applied to the recurrence $T(n) = 4T(n/2) + n^2 \log n$? Why or why not? Give an asymptotic upper bound for this recurrence.
- i) Apply dynamic programming technique in solving the travelling salesman problem.
- j) Write the solution of n -queen problem using the branch-and-bound technique.
- k) What do you mean by randomization? Write randomized quick sort algorithm and compare it with quick sort algorithm.

- I) Assume 3-SAT problem as an NP-complete problem, reduce Node cover decision problem to 3-SAT problem.

Part-III

Only Long Answer Type Questions (Answer Any Two out of Four)

- Q3 a** Using recurrence tree method, argue that the solution to the recurrence relation $T(n) = T(n/3) + T(2n/3) + cn$, where $c > 0$, is $\Omega(n \log n)$. **(8+8)**
- b** Show that the solution to $T(n)=2T(n/2)+n$ is $O(n \log n)$ using substitution method.
- Q4** Write the general steps of dynamic-programming paradigm to solve a problem. How is it different from the divide and conquer approach? Write pseudo code for dynamic-programming algorithm to solve 0-1 knapsack problem. What is the complexity of your algorithm? **(4+4+4+4)**
- Q5** What is a spanning tree? Write the pseudo code for finding the minimum spanning tree of a given graph using Prim's algorithm. Derive the time complexity of the algorithm. Use the algorithm to find the minimum spanning tree of the following graph. **(2+6+2+6)**



- Q6 a** Discuss the P, NP, NP-Hard and NP-Complete class of problems with suitable examples. **(8+8)**
- b** Define the node cover problem. Discuss a 2-approximation algorithm for node cover problem on the following graph.

